The Movie Database Case: A solution using the Maude-based e-Motions tool

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Abstract. The paper presents solutions for the TTC 2014 Movie Database Case, both in the e-Motions DSML and in the rewriting-logic formal language Maude. The DSLs defined in e-Motions are automatically transformed into Maude specifications, which are then used for simulation and analysis purposes. However, since e-Motions is a general purpose language, in which real-time languages may be modeled, with full support for OCL and other advanced features, the Maude specifications automatically generated are not as efficient as one would like. Since most of these features are not needed for the current tasks, we propose solutions both in e-Motions and in Maude, trying to highlight the main features of both languages. The fact that the solutions given directly in Maude lack the overhead included by e-Motions to deal with all those features it provides that are not needed in the current case study, makes these solutions much more efficient, and able to deal with bigger problems.

1 Introduction

Maude [3,4] is an executable formal specification language based on rewriting logic, which counts with a rich set of validation and verification tools [4,5], increasingly used as support to the development of UML, MDA, and OCL tools (see, e.g., [2, 14,6]). Furthermore, Maude has demonstrated to be a good environment for rapid prototyping, and also for application development (see surveys [4, 10]).

Maude may be seen as a general framework where to develop model transformations. Thus, Meseguer and Boronat use it to implement their model transformation framework MOMENT2; Durán, Vallecillo and others have used it to develop e-Motions [12], a tool that supports the definition and simulation of real-time Domain-Specific Modeling Languages (DSMLs); and similar approaches have later been used to give semantics to ATL [16] and other transformation languages.

The e-Motions tool is a DSML and graphical framework developed for Eclipse that supports the specification, simulation, and formal analysis of real-time systems. It provides a way to graphically specify the dynamic behavior of DSMLs using their concrete syntax, making this task quite intuitive. Furthermore, e-Motions behavioral specifications are models too, so that they can be fully integrated in MDE processes.

In e-Motions, MOF metamodels are formalized in rewriting logic, providing a representation of the structural aspects of any modeling language with a MOF metamodel. Then, given a description of the behavior of such modeling language as in-place transformation rules, e-Motions may be used to define both the syntax and the operational semantics of DSMLs. Artifacts developed in e-Motions are automatically translated into Maude.

As we will see in the following sections, e-Motions provides a very rich set of features, that enables the formal and precise definition of real-time DSMLs as models in a graphical and intuitive way. It makes use of an extension of in-place model transformation with a model of timed behavior and a mechanism to state action properties. The extension is defined in such a way that it avoids artificially modifying the DSML's metamodel to include time and action properties. Moreover, it supports attribute computations and ordered collections, which are specified by means of OCL expressions, thanks to mOdCL [13]. All these features makes the language very expressive, but directly impact on its performance. To gain an idea of this impact, we provide below solutions to the proposed problems both in e-Motions and directly in Maude and compare them.

The e-Motions system documentation and several examples are available at http://atenea.lcc.uma.es/e-Motions. The Maude web site is at http://maude.cs.uiuc.edu.

1.1 e-Motions

The definition of a Domain-Specific Language (DSL) typically comprises three tasks: (i) the definition of its abstract syntax, (ii) the definition of its concrete syntax and (iii) the specification of its behavior.

In e-Motions the abstract syntax is defined by means of an Ecore metamodel, in which all the language concepts and the relations between them are specified. The concrete syntax is provided by defining the so-called Graphical Concrete Syntax (GCS). A GCS is a model (conforms the GCS metamodel) where an image is attached to each concept defined in the abstract syntax.

In e-Motions the behavior of a DSL is specified using visual graph-transformation rules. An e-Motions rule consists of a Left-Hand Side (LHS), a Right-Hand Side (RHS) and zero or more Negative Application Conditions (NACs). The LHS defines a (sub)-graph matching, optionally conditional. The RHS specifies a (sub)-graph replacement, which if the rule is applied, every object in the LHS that is not in the RHS is deleted, new objects in the RHS that are not in the LHS are created, and those objects whose attributes (or links) are changed are updated. NACs specify conditions or (sub)-graphs such that if there is a matching, the rule cannot be fired.

Figure 1 shows an example of an e-Motions rule. The objects in both the RHS and LHS are represented by their associated images, as defined in the GCS model. Rule Assemble's LHS defines the precondition of the rule. It models an assemble machine who needs both a head and a handle in its connected conveyor. If NAC1, stating that the current matched Assemble object is not involved in other Assemble action, is not satisfied, the rule can be applied. The rule is

applied as follows. All objects in its LHS which do not appear in its RHS are deleted, i.e., objects he and ha. Those objects in its RHS which do not appear in its LHS are created, properly setting their attributes, i.e., the ham object with its three attributes. The rest of the objects remain changeless. Moreover, as e-Motions is a framework where to define real-time systems, each rule is applied in a established time, i.e. [prodTime,prodTime] in the Assemble rule. A rule with execution time [0,0] is considered instantaneous. A rule may contain zero or more local or auxiliary variables. All attribute or variable assignments and conditions are expressed using Object-Constraint Language (OCL) [11].

The abstract and concrete syntax, and the behavior of a DSL are models, and the e-Motions tool has been developed following MDE principles. The Maude code corresponding to a system defined in e-Motions is generated by an ATL/TCS transformation [15].

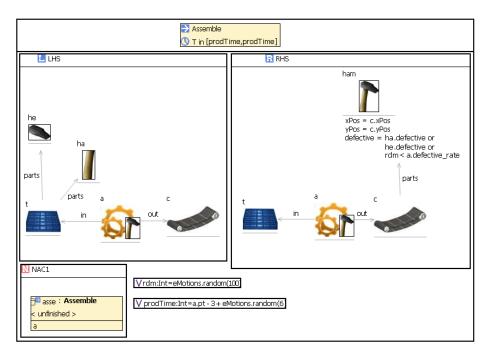


Fig. 1: e-Motions Assemble rule.

1.2 Rewriting Logic and Maude

Rewriting logic (RL) [9] is a logic of change that can naturally deal with state and with highly nondeterministic concurrent computations. In RL, the state space of a distributed system is specified as an algebraic data type in terms of an equational specification (Σ , E), where Σ is a signature of sorts (types) and

operations, and E is a set of equational axioms. The dynamics of a system in RL is then specified by rewrite rules of the form $t \to t'$, where t and t' are Σ -terms. This rewriting happens modulo the equations E, describing in fact local transitions $[t]_E \to [t']_E$. These rules describe the local, concurrent transitions possible in the system, i.e. when a part of the system state fits the pattern t (modulo the equations E) then it can change to a new local state fitting pattern t'. Notice the potential of this type of rewriting, and the very high-level of abstraction at which systems may be specified, to perform, e.g., rewriting modulo associativity or associativity-commutativity.

Maude [3,4] is a wide spectrum programming language directly based on RL. Thus, Maude integrates an equational style of functional programming with RL computation. Maude also supports the modeling of object-based systems by providing sorts representing the essential concepts of object (Object), message (Msg), and configuration (Configuration). A configuration is a multiset of objects and messages (with the empty-syntax, associative-commutative, union operator __) that represents a possible system state.

Although the user is free to define any syntax for objects and messages, several additional sorts and operators are introduced as a common notation. Maude provides sorts Oid for object identifiers, Cid for class identifiers, Attribute for attributes of objects, and AttributeSet for multisets of attributes (with _,_ as union operator). Given a class C with attributes a_i of types S_i , the objects of this class are then record-like structures of the form

$$< O : C \mid a_1 : v_1, ..., a_n : v_n > 0$$

where O is the identifier of the object, and v_i are the current values of its attributes (with appropriate types). See [4] for additional details on how object-oriented systems are represented in Maude, including explanations on how to represent inheritance, syntax for object-oriented modules, different forms of object communication, etc.

The following Maude definitions specify a class Account of bank accounts, with messages withdraw and transfer to operate with such bank accounts. The Account class is defined with a single attribute balance, of sort Int, representing the balance of an account. The withdraw message has two parameters, namely the addressee of the message and the amount of money to withdraw from the account. The transfer message will make the amount of money specified as its third argument to be transferred from the account given as first argument to the one given as second argument.

```
sort Account .
subsort Account < Cid .
op Account : -> Account .
op balance :_ : Int -> Attribute .
op withdraw : Oid Int -> Msg .
op transfer : Oid Oid Int -> Msg .
```

Rules debit and transfer below represent local transitions of the system that specify the behavior of bank accounts upon the reception of such messages. E.g.,

if an Account object receives a withdraw message and the amount of money to withdraw is smaller or equal than the balance of the account receiving the message, then the message is 'consumed' and the balance of the account is decremented is such an amount. Notice the synchronization of Account objects in the transfer rule.

Notice that, since the __ operator is declared associative, commutative, and with identity element, we do not need to worry about the order in which objects and messages appear in the rules. And since rules describe local transitions, we do not need to worry about the rest of the objects and messages in the configuration either.

Well-formedness of objects may be automatically checked by Maude's typing system. For example, we can add declarations constraining Account objects:

```
sort AccountObject .
subsort AccountObject < Object .

var O : Oid .
var Bal : Int .

mb < O : Account | balance : Bal > : AccountObject .
```

Notice that with these declarations, an object < O : Account | > is a valid term of sort Object, but since the membership cannot be applied on it, it is not of type AccountObject.

2 Solution

We are presenting two solutions for the different tasks, one graphical solution using e-Motions, and another one using directly Maude. Each task is solved by defining respective DSLs, which share their abstract and concrete syntaxes. The abstract syntax used is the one provided at [7] — we will see below that some of

the tasks have required extensions of this common syntax. The main differences between the DSLs defined for the different tasks is in their concrete behaviors describing what need to be done in each case, that is, the rewrite rules defining the behavior depends on the concrete task and its solution.

The e-Motions description of the different tasks is then transformed into a Maude specification and executed in Maude. We show how the formal tools available in Maude allow us to check the transformations carried out. Specifically, we will illustrate the use of Maude's reachability analysis capabilities to check that no undesired situation is reached along the execution.

Although the expressiveness of e-Motions is very welcome in complex problems, thanks to its capabilities to express problems visually, very intuitively and in a language very close to the problem domain, the overhead to be paid in cases like the ones at hand is too high. Specifically, the generality provided by its support for OCL expressions and time requirements, makes that the Maude code generated by the e-Motions tool is not as time performant as we would like. However, the general purpose rewrite-modulo engine at the core of Maude may also be used as a transformation language. Thus, together with the e-Motions solution we present an optimized Maude solution for each task.

As we will see below, the Maude version of the transformation closely follows the transformations provided in e-Motions, were all rewrite rules are *instantaneous* and expressions are solved directly by Maude built-in types instead of by the OCL interpreter [13]. Indeed, for problems as simple as the ones at hand, we will see that the representation distance between Maude and e-Motions to the problem domain would be very small, making both solutions very appropriate. Although a more in depth analysis of the problem at hand would most probably have allowed us to even improve the numbers obtained, we have preferred to keep the specification clear and intuitive.

2.1 Task 1

Task 1 comprises the generation of synthetic models (conforming the movie database metamodel [8]) from an input parameter $N \geq 0$. We first present an e-Motions solution and then a Maude solution.

e-Motions-based solution. Following an e-Motions based approach, we define the abstract and concrete syntax and the behavior of our so-called $Task\ 1\ DSL$. Taking a parameter N as input model, $Task\ 1\ DSL$ generates a model containing synthetic data.

As it has been introduced in Section 1.1, the abstract syntax of a DSL is given in e-Motions by means of an Ecore metamodel. Since we model the solution of the task as a model that evolves until reaching its final solution, we take as metamodel the one provided beforehand in [7], which we call *Movies MM*, extended with a Parameter concept. This results in a so-called *Movies* MM*. The class Parameter has two integer attributes, namely nP and nN, which represent positive graphs and negative graphs, respectively, for the generation following Henshin graphs [1].











(e) Parameter.

(a) Actor.

(b) Actress.

(c) Movie.

(d) Couple.

11.......* 1111

Fig. 2: Concrete syntax for *Movies* MM*.

For the concrete syntax, Figure 2 shows how an image has been attached to each concept modeled in the Movies* MM.

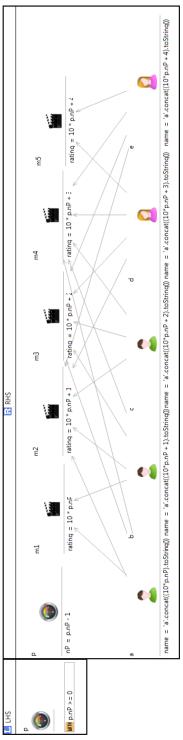
The behavior of this $Task\ 1\ DSL$ is then given by means of two in-place transformation rules: createPositive and createNegative. Figure 3a shows the createPositive rule, which takes an object p of type Parameter, with nP attribute greater or equal than 0, and produces synthetic data conforming to the Henshin rules [1]. Figure 3b shows the createNegative rule, which is analogously defined.

Once the syntax and the behavior of the system has been coded, the user may specify a model, which conforms to $Movies^*$ MM, containing an object Parameter with its two attributes nP and nN properly set. This model is used as initial model of the execution.

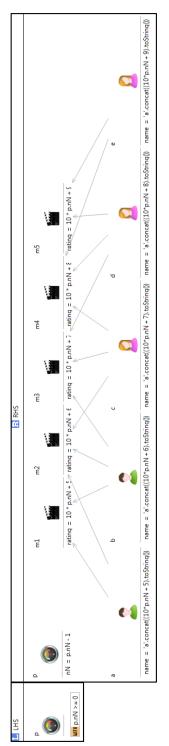
Please, note that this solution is really close to the problem specification in [8]. Figure 3 and [8, Figure 2], specifying the data generation, are almost the same. This demonstrates how close the solution by e-Motions is to the problem domain, and how convenient its graphical facilities are.

Maude solution. Our Maude-based solution for Task 1 consists of an object-based Maude specification, consisting of two modules: the MOVIES@MM module defining the classes structure, and the TASK1 module defining the rewrite rules to calculate the solution. As in the e-Motions solution, we have two rewrite rules: createPositive and createNegative. Listing 1.1 shows the createPositive Maude rule, that takes the createPositive(s(N:Nat)) message and a freshoid auxiliary message—used to create new object identifiers—and returns such a object configuration conforming the Henshin specification [8]. A similar rule generates the negative cases. Please notice that the Maude solution is very much like the e-Motions solution. In fact, the former could be seen as the textual version of the latter.

Listing 1.1: createPositive Maude rule.



(a) The createPositive rule.



(b) The negativePositive rule.

Fig. 3: Task 1 rules.

```
< N' + 3 : Movie | rating: (10.0 * float(N) + 3.0) >
< N' + 4 : Movie \mid rating: (10.0 * float(N) + 4.0) >
< N' + 5 : Actor | name: ("a" + string(10 * N, 10)),
                 movies: (N', N' + 1, N' + 2, N' + 3) >
                         ("a" + string(10 * N + 1, 10)),
< N' + 6 : Actor | name:
                         (N', N' + 1, N' + 2) >
                 movies:
                         ("a" + string(10 * N + 2, 10)),
< N' + 7 : Actor | name:
                 movies: (N' + 1, N' + 2, N' + 3) >
    + 8 : Actress \mid name: ("a" + string(10 * N + 3, 10)),
                 movies: (N' + 1, N' + 2, N' + 3, N' + 4) >
    + 9 : Actress \mid name: ("a" + string(10 * N + 4, 10)),
                 movies: (N' + 1, N' + 2, N' + 3, N' + 4) >
freshOid(N' + 10)
```

Execution performance for both solutions. Table 1 shows the number of rewrites and execution times for both solutions. As explained above, the execution times for the Maude specification obtained from the e-Motions definition grows very quickly. Notice that, although the number of rewrites grows linearly with respect to N, the time is exponential due to the infrastructure to deal with all the extra features in e-Motions. However, notice how the number of rewrites for the Maude solution grows linearly as well, but in this case the execution times grow more slowly, being able to handle problems of much bigger sizes.

On the correctness of the transformation Maude provides a whole formal environment where we can perform proofs of correctness of our solutions. In addition to tools to verify the termination, confluence, etc. of our rewrite systems, Maude provides a reachability analysis tool and a model checker, which are particularly convenient for performing checks on the correctness of systems. Let us consider here the Maude search command, which allows us to explore the whole reachable state space, or up to a given depth, looking for states satisfying a given condition.

For instance, following the results given in [8], for some N, the above rules createPositive and createNegative create 20N objects, specifically, 10N movies, 5N actresses, and 5N actors. We could check that the solution found satisfies this condition, but we can do something more interesting by checking that no final reachable state fails to satisfy it. Of course, if the rewrite system is confluent and terminating the solution would be unique.

Given the numOfMovies operation, which takes an object configuration as input and returns the number of movies in it, we may look for those final states in which the number of movies will be different than 10N:

```
search createPositive(8) createNegative(8) freshOid(0)
=>! C:Configuration
such that numOfMovies(C:Configuration) =/= 10 * 8 .
```

	e-Motions		Maude	
N	Time (s)	# Rewrites	Time (s)	# Rewrites
1			0.0	67
2	0.0	4,910	0.0	133
10	0.0	24,334	0.0	661
20	0.0	48,614	0.0	1321
100	0.6	242,854	0.0	6601
1000	55.7	2,428,054	1.7	66,001
2000	395.0	4,856,054	11.8	132,001
3000			31.5	198,001
4000			40.8	264,001
5000			65.8	330,001
6000			96.8	396,001
7000			133.4	462,001
8000			175.8	528,001
9000			224.5	594,001
10000			227.9	660,001
11000			337.4	726,001

Table 1: Times for the e-Motions and Maude solutions to Task 1

The arrow =>! means that it search for final states, that is, states that cannot be further rewritten, starting from the given initial configuration, that satisfy the given condition. Maude returns no solution for the above code, that means all final states reached have exactly 10 movies:

No solution.

2.2 Task 2

Task 2 consists in finding all 'couples' from a given model, given that two persons are a 'couple' if they played together in at least three movies [8]. Couples are to be obtained either from the model obtained in Task 1 or from the IMBd database [7]. Once again, we present solutions using e-Motions and Maude.

e-Motions-based solution. The solution for this task is implemented with one single rule, createCouple, shown in Fig. 4. Person objects are shown using square shapes because Person is an abstract class and it does not have attached image. The createCouple rule models the creation of a couple by taking two persons and generating a couple with them. The rule has two conditions: a positive condition stating that "the number of movies in the intersection between the movies of per1 and per2 is greater or equal than 3"; and a negative condition,

N	Time (s)	# Rewrites
2	0.7	524,781
10	46.7	19,453,091
20	660.1	161,741,321

Table 2: e-Motions times for Task 2 First Version.

the coupleHasNotBeenCreated NAC, requiring that the couple does not exists yet.

Although very intuitive and simple, this solution is computationally very expensive. Notice that the number of matchings in the LHS of the rule is combinatorial, leaving all the task to the evaluation of the conditions to accept or discard the couples.

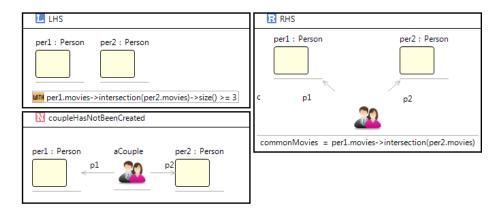


Fig. 4: createCouple rule.

We have implemented another solution in which we limit the number of matchings using a very simple algorithm: For each person, we iterate on the rest of persons looking for couples. With this algorithm, the number of persons to match as candidate couples decreases significantly. To model this solution, we extend the metamodel and its concrete syntax with a so-called Collection concept. This class has three attributes, namely people, with the set of persons to be handled, fixedPerson, to iterate on each person, and peopleDealtWith, to keep the persons already considered to create a couple with the current 'fixed person'. Figures 5-9 show the rules specifying this solution:

- Rule initialRule in Figure 5 initializes the collection object assigning the set of all actors and actresses to its people attribute (the other attributes

- get default values). This rule is only fired if there is no collection object in the model.
- Rule fixPerson in Figure 6 takes a person from the people set and takes it as fixedPerson. Notice that p is removed from the people set.
- Rules doingCouples-AreCouple and doingCouples-AreNotCouple in Figures 7 and 8 take a person from the set people and the fixedPerson and make a couple if the number of movies they share is greater or equal than three. In both cases the person considered is passed to the peopleDealtWith set.
- When all persons has been considered as couple of the current fixedPerson, the nextPerson rule in Figure 9, takes the peopleDealtWith as new people set.



Fig. 5: initialRule rule.

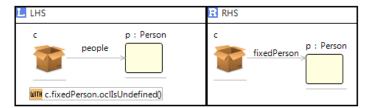
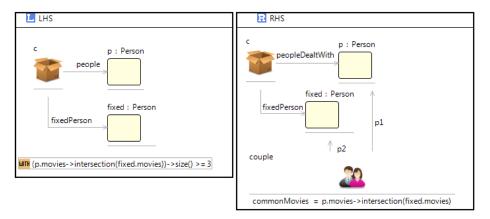


Fig. 6: fixPerson rule.

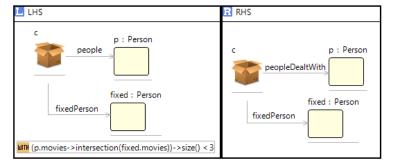
Maude-based solution. Again, we specify directly in Maude both solutions. As for Task 1, the solutions match very closely their e-Motions counterparts.

The Maude specification of the first alternative solution to Task 1 is shown in Listing 1.2. The rules takes two persons and creates a new couple if they share three movies and such couple has not been previously created. Some numbers for its execution are shown in Table 3.

Listing 1.2: createCouples Maude rule.



 $Fig.\,7: {\tt doingCouples-AreCouple}\ rule.$



 $Fig.\,8: \\ \verb|doingCouples-AreNotCouple| rule.$

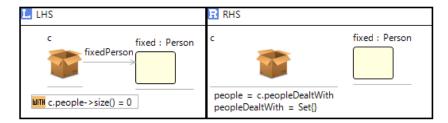


Fig. 9: nextPerson rule.

N	Time (s)	# Rewrites
1	0.0	8,680
5	0.5	1,343,000
10	5.0	11,020,000
20	66.3	89,276,000
30	314.0	302,568,000

Table 3: Maude times for Task 2 First Version.

As for e-Motions, the second solution consists of several rules. In this case, our collection object is model by an operator $\{-\}\{-\}\{-\}\{-\}\{-\}\{-\}\}$ representing an object with six attributes as its e-Motions counterpart: its arguments take, respectively, the starting argument, the people set, the movies set, the dealt people, the fixed person on which to iterate, and the result configuration. We show in Listing 1.3 the code for the doingPairs rule. In the case of Maude, we only need one rule to consider the positive and negative cases. The number of rewrites and execution times for executions of different sizes are shown in Table 4.

Listing 1.3: doingCouples Maude rule.

N	Time (s)	# Rewrites
1	0.0	831
10	0.1	82,983
100	8.9	8,299,803
200	68.3	33,199,603
300	242.9	74,699,403
400	640.1	$132,\!799,\!203$

Table 4: Maude times for Task 2 Second Version.

2.3 Task 3

Given a model with couples already created, Task 3 consists in calculating the average rating of shared movies for each of these couples. As for the previous tasks, we provide solutions both in e-Motions and Maude.

e-Motions-based solution. The solution consists in one single rule, shown in Figure 10, in which the average is calculated only once for each couple. Notice the use of an action in the NAC of the rule to state that the value has not been already calculated. The number of rewrites and execution times for N=2,10 are shown in Table 5.

Maude-based solution. The corresponding Maude rule specifying the solution of this task is shown in Listing 1.4. Table 6 show the number of rewrites and execution times for problems of sizes 100, 200, 300, and 400.



Fig. 10: computingAvgRating rule.

N	Time (s)	# Rewrites
2	0.0	4,527
10	2.1	891,432

Table 5: e-Motions times for Task 3.

Listing 1.4: Maude rule for Task 3 solution.

N	Time (s) #	${\bf Rewrites}$
100	1.5	21,800
200	6.3	43,600
300	14.9	$65,\!400$
400	29.7	87,200

Table 6: Maude times for Task 3.

3 Conclusions

We have presented solutions for the TTC 2014 Movie Database Case both in the e-Motions DSML and in the rewriting-logic formal language Maude.

e-Motions provides a very rich set of features, that enables the formal and precise definition of real-time DSMLs as models in a graphical and intuitive way. It makes use of an extension of in-place model transformation with a model of timed behavior and a mechanism to state action properties. The extension is defined in such a way that it avoids artificially modifying the DSML's metamodel to include time and action properties. Moreover, it supports attribute computations and ordered collections, which are specified by means of OCL expressions. All these features makes the language very expressive, but directly impact on performance.

The Maude solutions presented are also very intuitive and simple. The fact that the solutions given directly in Maude lack the overhead included by e-Motions to deal with all those features it provides that are not needed in the current case study, makes the solutions given much more efficient, and able to deal with bigger problems.

We believe that the Maude solutions could still be made more efficient, but possibly at the cost of loosing elegance in the solutions.

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